2017.6 | Transformer

Solely based on attention mechanism, the Transformer is proposed and shows great performance on NLP tasks.

2020.5 | GPT-3

A huge transformer with 170B parameters, takes a big step towards general NLP model.

2020.10 | VIT

Pure transformer architectures work well for visual recognition.

2021 | ViT Variants

Variants of ViT models, e.g., DeiT, PVT, TNT, and Swin.

2023 | GPT4

A generalized multimodal model for both language and vision tasks.

2018.10 | BERT

Pre-training transformer models begin to be dominated in the field of NLP.

2020.5 | DETR

A simple yet effective framework for high-level vision by viewing object detection as a direct set prediction problem.

End of 2020 | IPT/SETR/CLIP

Applications of transformer model on low-level vision, segment and multimodal tasks, respectively.

2022 | DALLE2/StableDiffsusion

Generating high-quality images from natural language descriptions with diffusion models.

Fig. 1: Key milestones in the development of transformer. The vision transformer models are marked in red.

Published as a conference paper at ICLR 2021

AN IMAGE IS WORTH 16x16 WORDS: TRANSFORMERS FOR IMAGE RECOGNITION AT SCALE

Alexey Dosovitskiy*,†, Lucas Beyer*, Alexander Kolesnikov*, Dirk Weissenborn*, Xiaohua Zhai*, Thomas Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, Jakob Uszkoreit, Neil Houlsby*,†

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Google Research, Brain Team
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ABSTRACT

While the Transformer architecture has become the de-facto standard for natural language processing tasks, its applications to computer vision remain limited. In vision, attention is either applied in conjunction with convolutional networks, or used to replace certain components of convolutional networks while keeping their overall structure in place. We show that this reliance on CNNs is not necessary and a pure transformer applied directly to sequences of image patches can perform very well on image classification tasks. When pre-trained on large amounts of data and transferred to multiple mid-sized or small image recognition benchmarks (ImageNet, CIFAR-100, VTAB, etc.), Vision Transformer (ViT) attains excellent results compared to state-of-the-art convolutional networks while requiring substantially fewer computational resources to train.

Part 1. Hight Level Overview

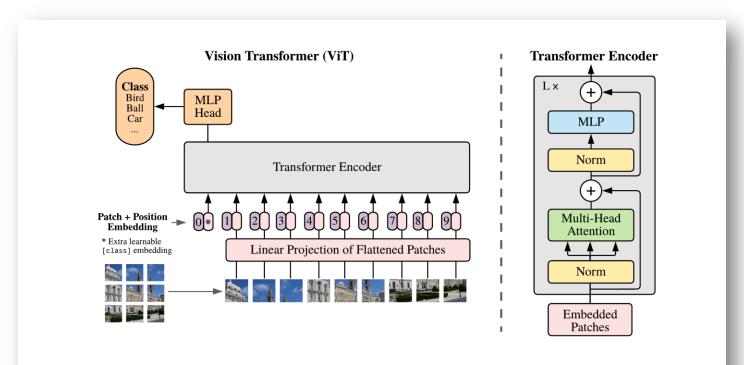
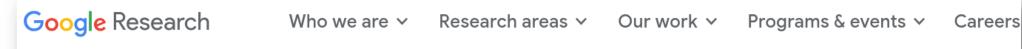


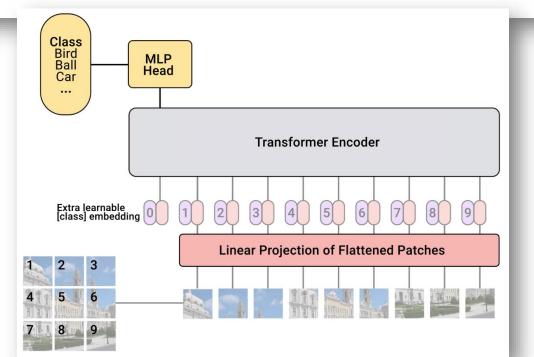
Figure 1: Model overview. We split an image into fixed-size patches, linearly embed each of them, add position embeddings, and feed the resulting sequence of vectors to a standard Transformer encoder. In order to perform classification, we use the standard approach of adding an extra learnable "classification token" to the sequence. The illustration of the Transformer encoder was inspired by Vaswani et al. (2017).

http://research.google/blog/transformers-for-image-recognition-at-scale/

https://1.bp.blogspot.com/- mnVfmzvJWc/X8gMzhZ7SkI/AAAAAAAAAG24/8gW2AHEoqUQrBwOqjhYB37A7OOjNyKuNgCLcBGAsYHQ/s1600/image1.gif



ViT divides an image into a grid of square patches. Each patch is flattened into a single vector by concatenating the channels of all pixels in a patch and then linearly projecting it to the desired input dimension. Because Transformers are agnostic to the structure of the input elements we add learnable position embeddings to each patch, which allow the model to learn about the structure of the images. *A priori*, ViT does not know about the relative location of patches in the image, or even that the image has a 2D structure — it must learn such relevant information from the training data and encode structural information in the position embeddings.



High Level Overview

 in general (not only for ViT) we create a network from blocks that consists of several layers

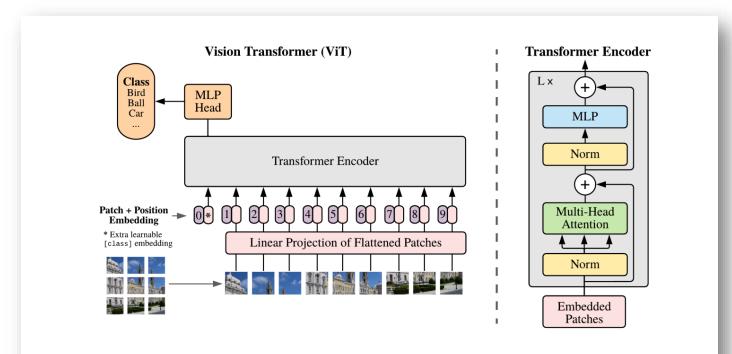


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- e.g. inception blocks, residual blocks, transformer encoder blocks
- what is input for these models (blocks)?

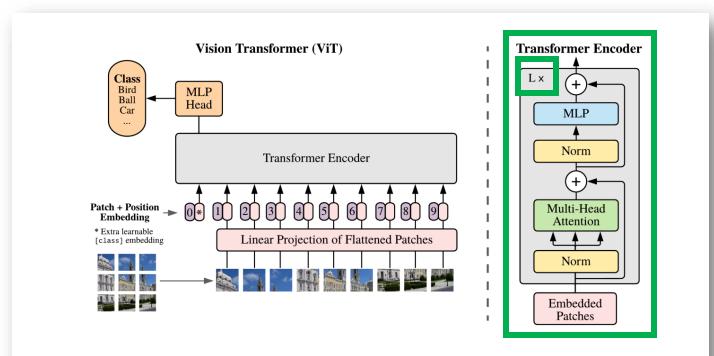


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- in general (not only for ViT) we create a network from blocks that consists of several layers
- e.g. inception blocks, residual blocks, transformer encoder blocks
- what is input for these models (blocks)?
- In the case of CNN, we use raw images
- In the case of ViT, we use fixed size patches

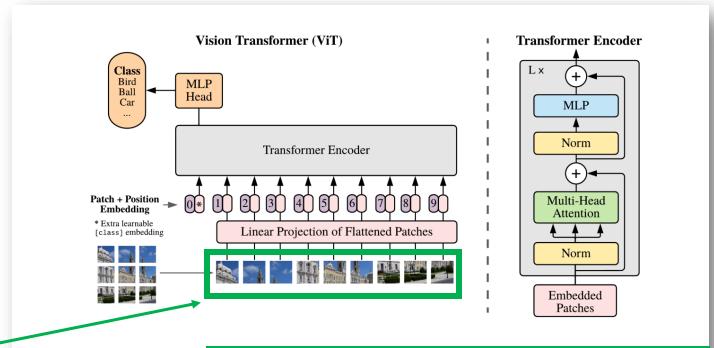


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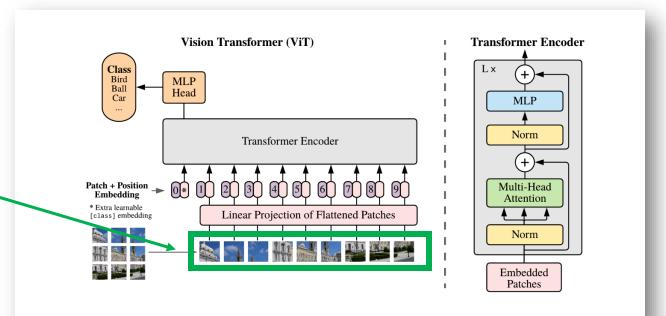


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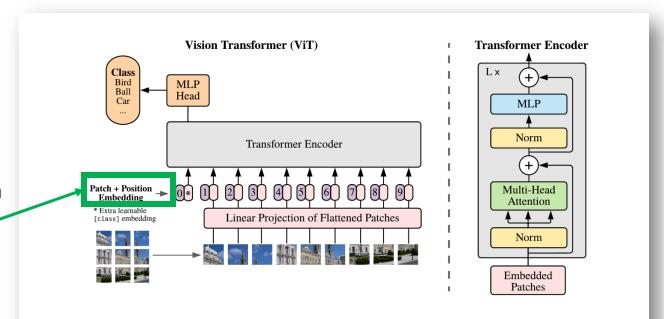


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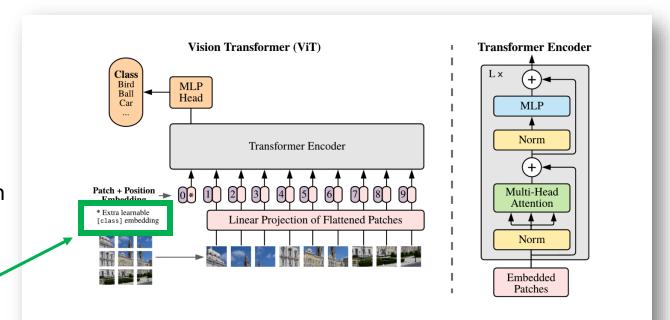


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- The Transformer encoder processes enables each
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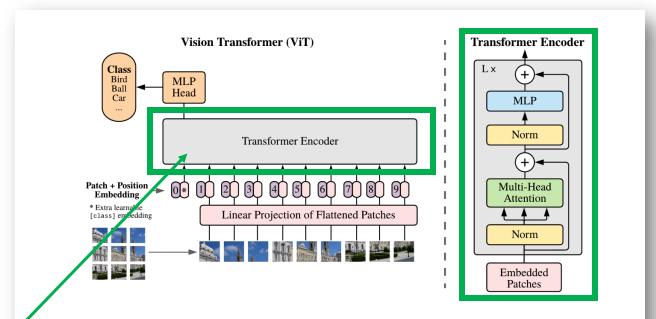


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- 4. The Transformer encoder processes enables each token to attend to every other token
- 5. Classification Head output predictions based on *I* the classification token.

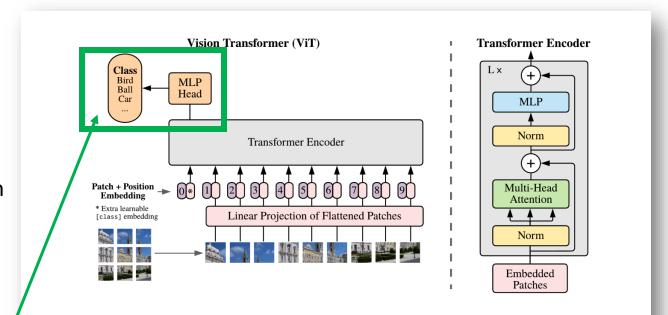


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Model	Layers	Hidden size D	MLP size	Heads	Params
ViT-Base	12	768	3072	12	86M
ViT-Large	24	1024	4096	16	307M
ViT-Huge	32	1280	5120	16	632M

Table 1: Details of Vision Transformer model variants.



Part 2. A Bit More Detail

LayerNorm

CLASS torch.nn.LayerNorm(normalized_shape, eps=1e-05, elementwise_affine=True, bias=True, device=None, dtype=None) [SOURCE]

Applies Layer Normalization over a mini-batch of inputs.

This layer implements the operation as described in the paper Layer Normalization

$$y = \frac{x - \mathrm{E}[x]}{\sqrt{\mathrm{Var}[x] + \epsilon}} * \gamma + \beta$$

The mean and standard-deviation are calculated over the last D dimensions, where D is the dimension of normalized_shape. For example, if normalized_shape is (3, 5) (a 2-dimensional shape), the mean and standard-deviation are computed over the last 2 dimensions of the input (i.e. input.mean((-2, -1))). γ and β are learnable affine transform parameters of normalized_shape if elementwise_affine is True. The standard-deviation is calculated via the biased estimator, equivalent to torch.var(input,unbiased-False).

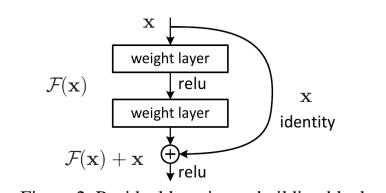
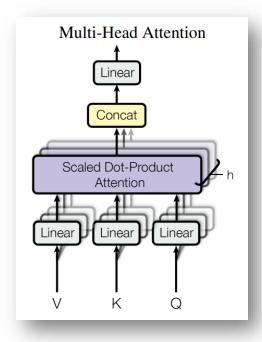


Figure 2. Residual learning: a building block.



Step 1 - Input

- transform image into 16 x 16 size (patches)
- embed each patch into 768 dimension
- i.e. one patch can be described with 1 x 768 values
- In the case that we have 196 patches with size of 16 x 16, we obtain [14, 14, 768] tensor
- with the use of flatten, we obtain [196, 768] matrix

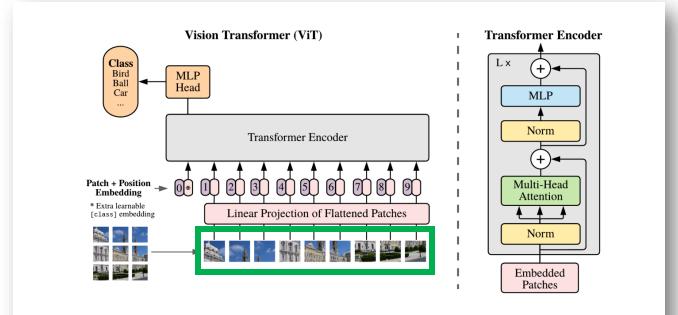


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- 10, we obtain [14, 14, 708] tensor

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An overview of the model is depicted in Figure 1. The star

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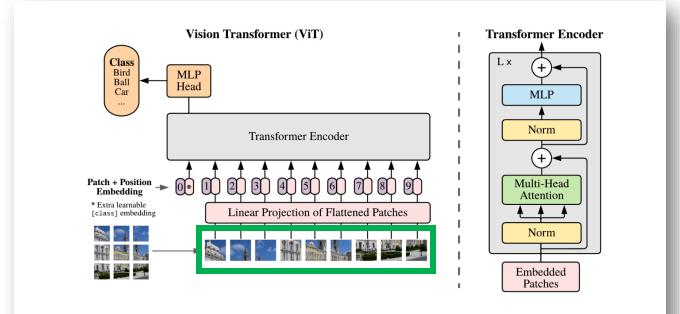


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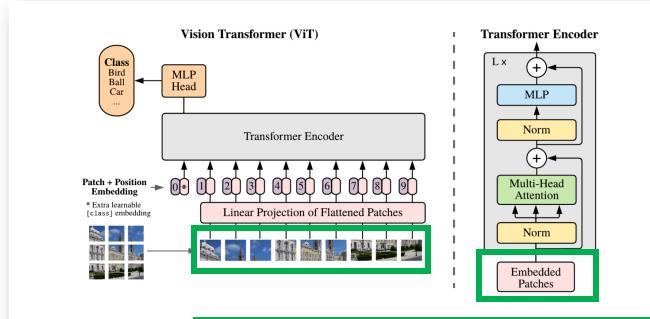


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$$\mathbf{z}_{0} = [\mathbf{x}_{\text{class}}; \mathbf{x}_{p}^{1}\mathbf{E}; \mathbf{x}_{p}^{2}\mathbf{E}; \cdots; \mathbf{x}_{p}^{N}\mathbf{E}] + \mathbf{E}_{pos}, \qquad \mathbf{E} \in \mathbb{R}^{(P^{2} \cdot C) \times D}, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$$

$$\mathbf{z}'_{\ell} = \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1}, \qquad \ell = 1 \dots L$$

$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z}'_{\ell})) + \mathbf{z}'_{\ell}, \qquad \ell = 1 \dots L$$

$$\mathbf{y} = \text{LN}(\mathbf{z}_{L}^{0})$$

$$\mathbf{v}_{\text{ision Transformer (ViT)}}$$

$$\mathbf{v}_{\text{ision Transformer Encoder}}$$

$$\mathbf{v}_{\text{ision Transformer Encoder}}$$

$$\mathbf{v}_{\text{init}} + \mathbf{v}_{\text{osition}}$$

$$\mathbf{v}_{\text{osition}} + \mathbf{v}_{\text{osition}}$$

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Patches

$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \mathbf{x}_p^1 \mathbf{E}; \, \mathbf{x}_p^2 \mathbf{E}; \cdots; \, \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos},$$

$$\mathbf{E} \in \mathbb{R}^{(P^2 \cdot C) \times D}, \ \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$$

$$\mathbf{z'}_{\ell} = \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1},$$

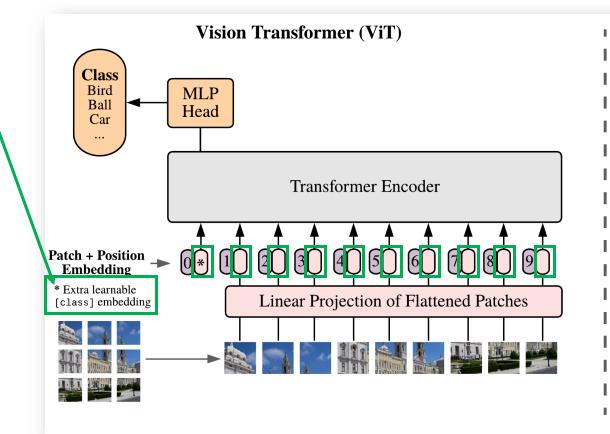
$$\ell = 1 \dots L \tag{2}$$

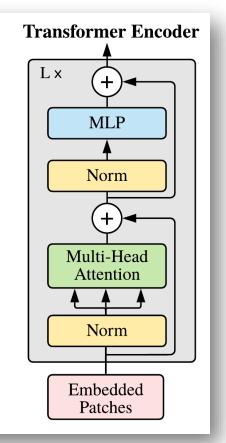
$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z'}_{\ell})) + \mathbf{z'}_{\ell},$$

$$\ell = 1 \dots L$$

 $\mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$

For classification purposes, the same as the class token used in BERT.



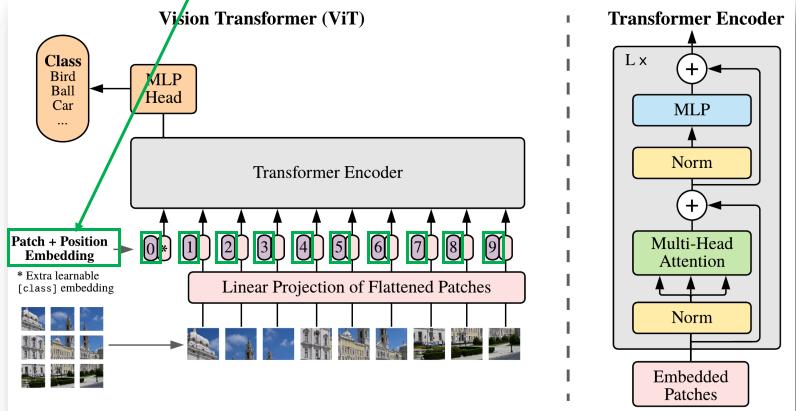


(4)

(3)

(1)

$$\begin{aligned} \mathbf{z}_0 &= [\mathbf{x}_{\text{class}}; \ \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{x}_p^2 \mathbf{E}; \cdots; \ \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos}, \\ \mathbf{z}'_{\ell} &= \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1}, \\ \mathbf{z}_{\ell} &= \text{MLP}(\text{LN}(\mathbf{z}'_{\ell})) + \mathbf{z}'_{\ell}, \\ \mathbf{y} &= \text{LN}(\mathbf{z}_L^0) \end{aligned} \qquad \begin{aligned} \mathbf{E} &\in \mathbb{R}^{(P^2 \cdot C) \times D}, \ \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D} \\ \ell &= 1 \dots L \end{aligned}$$



(1)

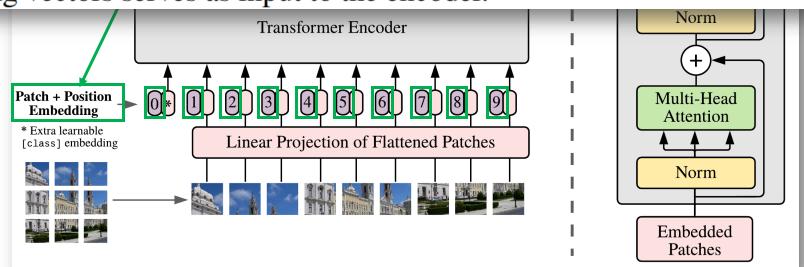
(2)

(3)

(4)

$$\mathbf{z}_{0} = [\mathbf{x}_{\text{class}}; \mathbf{x}_{p}^{1}\mathbf{E}; \mathbf{x}_{p}^{2}\mathbf{E}; \cdots; \mathbf{x}_{p}^{N}\mathbf{E}] + \mathbf{E}_{pos}, \qquad \mathbf{E} \in \mathbb{R}^{(P^{2} \cdot C) \times D}, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$$
(1)
$$\mathbf{z}'_{\ell} = \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1}, \qquad \ell = 1 \dots L$$
(2)
$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z}'_{\ell})) + \mathbf{z}'_{\ell}, \qquad \ell = 1 \dots L$$
(3)

Position embeddings are added to the patch embeddings to retain positional information. We use standard learnable 1D position embeddings, since we have not observed significant performance gains from using more advanced 2D-aware position embeddings (Appendix D.4). The resulting sequence of embedding vectors serves as input to the encoder.



$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \ \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{x}_p^2 \mathbf{E}; \cdots; \ \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos},$$

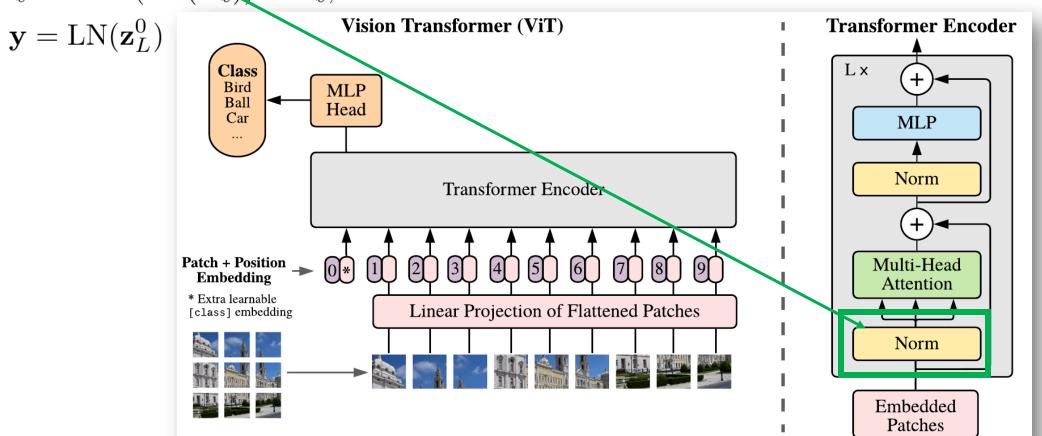
$$\mathbf{E} \in \mathbb{R}^{(P^2 \cdot C) \times D}, \, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D} \tag{1}$$

$$\mathbf{z}'_{\ell} = \text{MSA}(\mathbf{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1},$$

$$\ell=1\dots L$$

$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z'}_{\ell})) + \mathbf{z'}_{\ell},$$

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(4)

(2)

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$$\mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$$

Patch + Position
Embedding
* Extra learnable

[class] embedding

Difference between Batch Normalization and Layer Normalization

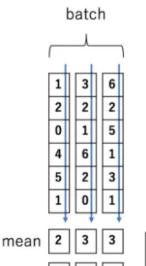
BatchNorm normalizes each feature within a batch of samples, while LayerNorm normalizes all features within each sample.

Let's assume we have a two-dimensional input matrix, where the rows represent the batch and the columns represent the sample features. The target of Batch Normalization is a batch of samples, and the target of Layer

Vision Tra Normalization is a single sample, Figure 1 illustrates this concept:

Batch Normalization

Layer Normalization



Same for all feature dimensions

https://medium.com/@florian_algo/batchnorm-and-layernorm-2637f46a998b

Li

(1)

(2)

(3)

(4)

LayerNorm

$$egin{aligned} \mathbf{z}_0 &= [\mathbf{x}_{ ext{class}}; \ \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{z'}_\ell &= \operatorname{MSA}[\operatorname{LN}(\mathbf{z}_\ell) \ \mathbf{z}_\ell &= \operatorname{MLP}(\operatorname{LN}(\mathbf{z'}_\ell) \ \mathbf{y} &= \operatorname{LN}(\mathbf{z}_L^0) \end{aligned}$$

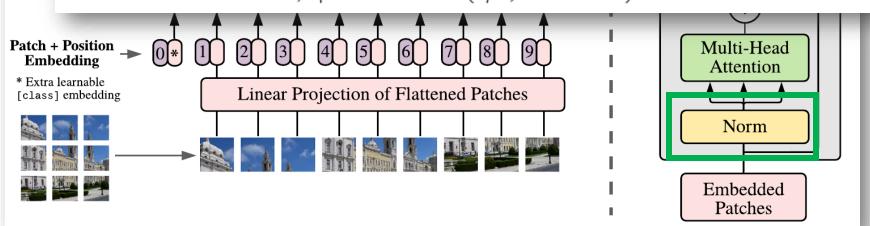
CLASS torch.nn.LayerNorm(normalized_shape, eps=1e-05, elementwise_affine=True, bias=True, device=None, dtype=None) [SOURCE]

Applies Layer Normalization over a mini-batch of inputs.

This layer implements the operation as described in the paper Layer Normalization

$$y = \frac{x - \mathrm{E}[x]}{\sqrt{\mathrm{Var}[x] + \epsilon}} * \gamma + \beta$$

The mean and standard-deviation are calculated over the last D dimensions, where D is the dimension of normalized_shape. For example, if normalized_shape is (3, 5) (a 2-dimensional shape), the mean and standard-deviation are computed over the last 2 dimensions of the input (i.e. input.mean((-2, -1))). γ and β are learnable affine transform parameters of normalized_shape if elementwise_affine is True. The standard-deviation is calculated via the biased estimator, equivalent to torch.var(input, unbiased=False).



24

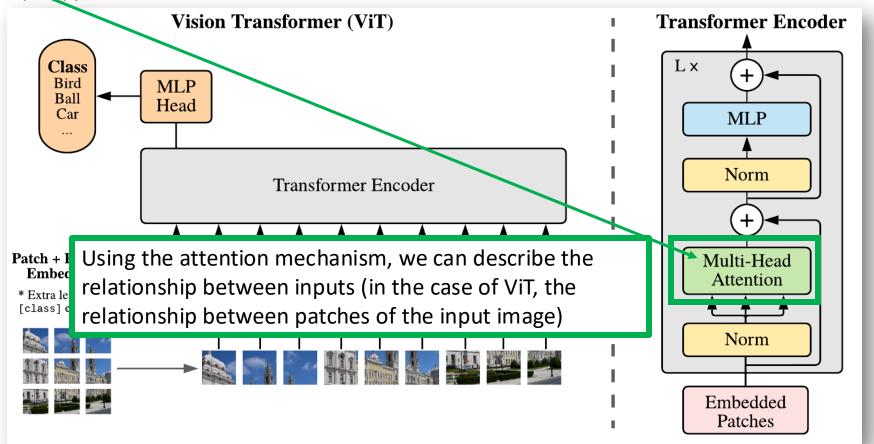
$$\mathbf{z}_{0} = [\mathbf{x}_{\text{class}}; \, \mathbf{x}_{p}^{1}\mathbf{E}; \, \mathbf{x}_{p}^{2}\mathbf{E}; \cdots; \, \mathbf{x}_{p}^{N}\mathbf{E}] + \mathbf{E}_{pos}, \qquad \mathbf{E} \in \mathbb{R}^{(P^{2} \cdot C) \times D}, \, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$$

$$(1)$$

$$\mathbf{z}'_{\ell} = MSA(LN(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1}, \qquad \ell = 1...L$$
 (2)

$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z}'_{\ell})) + \mathbf{z}'_{\ell}, \qquad \ell = 1 \dots L$$
 (3)





(4)

Self attention was proposed in https://arxiv.org/pdf/1706.03762

$$\mathbf{E} \in \mathbb{R}^{(P^2 \cdot C) \times D}, \, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$$
(1)

Following text was taken from https://arxiv.org/pdf/2012.12556

$$=1\dots L$$
 (2)

2.1 Self-Attention

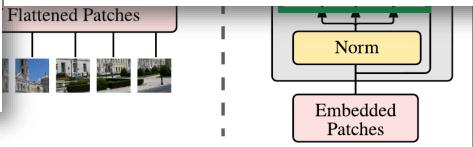
In the self-attention layer, the input vector is first transformed into three different vectors: the query vector \mathbf{q} , the key vector \mathbf{k} and the value vector \mathbf{v} with dimension $d_q = d_k = d_v = d_{model} = 512$. Vectors derived from different inputs are then packed together into three different matrices, namely, \mathbf{Q} , \mathbf{K} and \mathbf{V} . Subsequently, the attention function between different input vectors is calculated as follows (and shown in Figure 3 left):

- Step 1: Compute scores between different input vectors with $S = Q \cdot K^{\top}$;
- Step 2: Normalize the scores for the stability of gradient with $S_n = S/\sqrt{d_k}$;
- Step 3: Translate the scores into probabilities with softmax function $P = \operatorname{softmax}(S_n)$;
- Step 4: Obtain the weighted value matrix with $\mathbf{Z} = \mathbf{V} \cdot \mathbf{P}$.

The process can be unified into a single function:

Attention(
$$\mathbf{Q}, \mathbf{K}, \mathbf{V}$$
) = softmax($\frac{\mathbf{Q} \cdot \mathbf{K}^{\top}}{\sqrt{d_k}}$) · \mathbf{V} . (1)

The logic behind Eq. T is simple. Step 1 computes scores between each pair of different vectors, and these scores determine the degree of attention that we give other words when encoding the word at the current position. Step 2 normalizes the scores to enhance gradient stability for improved training, and step 3 translates the scores into probabilities. Finally, each value vector is multiplied by the sum of the probabilities. Vectors with larger probabilities receive additional focus from the following layers.



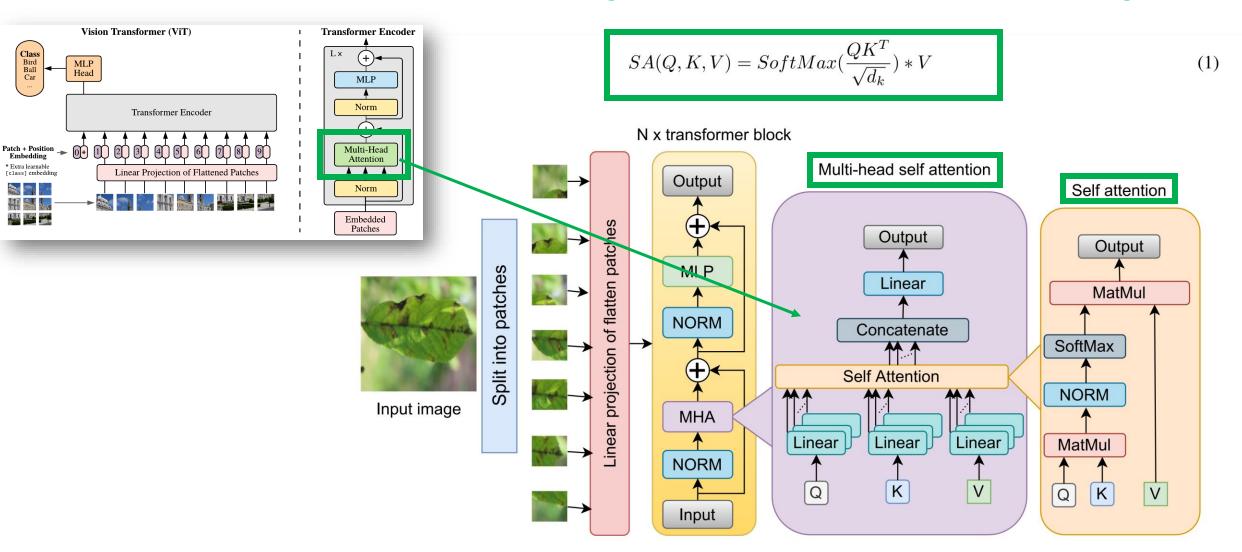


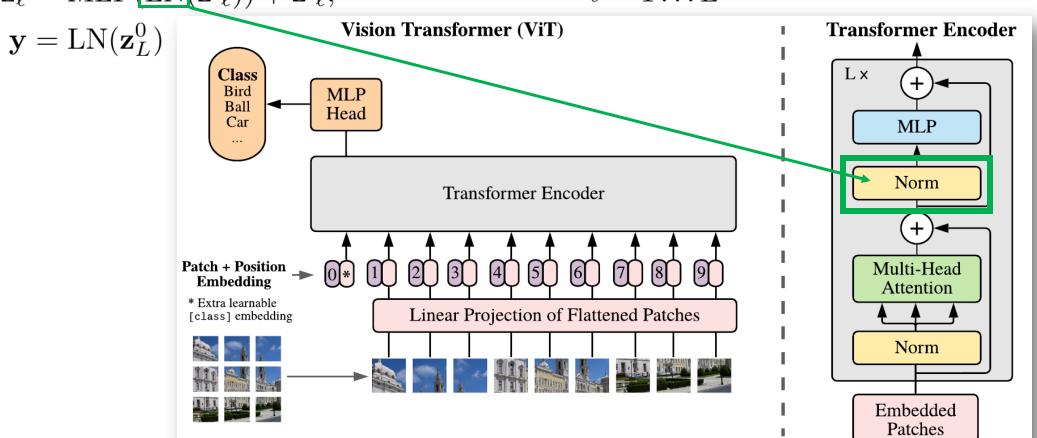
Figure 1: ViT block with multi-head self-attention block and self-attention

$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \, \mathbf{x}_p^1 \mathbf{E}; \, \mathbf{x}_p^2 \mathbf{E}; \cdots; \, \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos}, \qquad \mathbf{E} \in \mathbb{R}^{(P^2 \cdot C) \times D}, \, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$$

$$\mathbf{z}'_{\ell} = \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1},$$
 $\ell = 1 \dots L$ (2)

$$\mathbf{z}_{\ell} = \text{MLP}(\mathbf{LN}(\mathbf{z'}_{\ell})) + \mathbf{z'}_{\ell},$$

$$\ell = 1 \dots L$$



(1)

(3)

(4)

$$\mathbf{z}_{0} = [\mathbf{x}_{\text{class}}; \ \mathbf{x}_{p}^{1}\mathbf{E}; \ \mathbf{x}_{p}^{2}\mathbf{E}; \cdots; \ \mathbf{x}_{p}^{N}\mathbf{E}] + \mathbf{E}_{pos}, \qquad \mathbf{E} \in \mathbb{R}^{(P^{2} \cdot C) \times D}, \ \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D} \tag{1}$$

$$\mathbf{z}'_{\ell} = \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1}, \qquad \ell = 1 \dots L \tag{2}$$

$$\mathbf{z}_{\ell} = \underline{\text{MLP}}(\text{LN}(\mathbf{z}'_{\ell})) + \mathbf{z}'_{\ell}, \qquad \ell = 1 \dots L \tag{3}$$

$$\mathbf{y} = \text{LN}(\mathbf{z}_{L}^{0})$$

$$\mathbf{y} = \text{LN}(\mathbf{z}_{L}^{0})$$

$$\mathbf{y} = \frac{\mathbf{E}_{\text{ninedding}}}{\mathbf{E}_{\text{ninedding}}}$$

$$\mathbf{E}_{\text{Entedding}}$$

$$\mathbf{E}_{\text{Entedding}}$$

$$\mathbf{E}_{\text{Extra learnable class}}$$

$$\mathbf{E}_{\text{enteddedd}}$$

$$\mathbf{E}_{\text{Embeddedd}}$$

$$\mathbf{E}_{\text{enteddedd}}$$

$$\mathbf{E}_{\text{enteddedd}}$$

$$\mathbf{E}_{\text{enteddedd}}$$

$$\mathbf{E}_{\text{enteddedd}}$$

$$\mathbf{E}_{\text{enteddedd}}$$

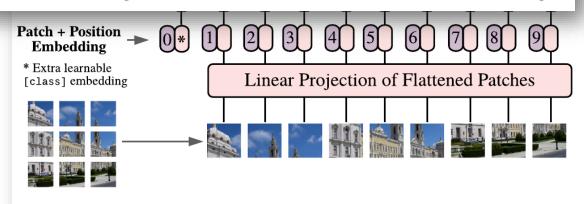
$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \, \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{z'}_\ell = \mathrm{MSA}(\mathrm{LN}(\mathbf{z}_\ell), \ \mathbf{z}_\ell = \mathrm{MLP}(\mathrm{LN}(\mathbf{z'}_\ell), \ \mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$$

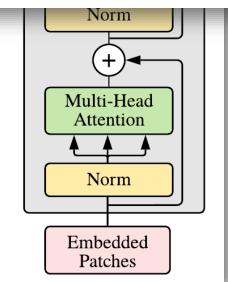
This block implements the multi-layer perceptron (MLP) module.

Parameters:

- in_channels (int) Number of channels of the input
- hidden_channels (List[int]) List of the hidden channel dimensions

The MLP contains two layers with a GELU non-linearity.





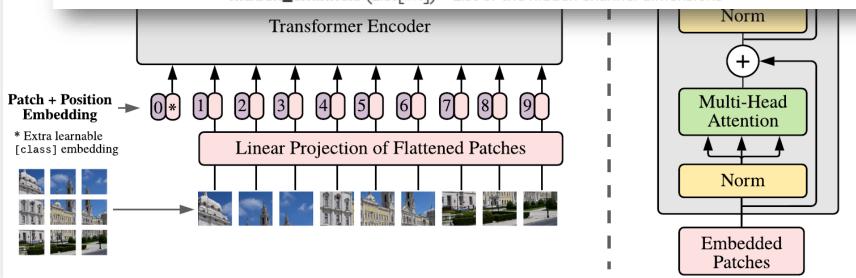
$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \, \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{z'}_\ell = \mathrm{MSA}(\mathrm{LN}(\mathbf{z}_\ell), \ \mathbf{z}_\ell = \mathrm{MLP}(\mathrm{LN}(\mathbf{z'}_\ell), \ \mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$$

```
torchvision.ops.MLP(in_channels: int, hidden_channels: ~typing.List[int],
norm_layer: ~typing.Optional[~typing.Callable[[...],
~torch.nn.modules.module.Module]] = None, activation_layer:
~typing.Optional[~typing.Callable[[...], ~torch.nn.modules.module.Module]] =
<class 'torch.nn.modules.activation.ReLU'>, inplace: ~typing.Optional[bool] =
None, bias: bool = True, dropout: float = 0.0) [SOURCE]
```

This block implements the multi-layer perceptron (MLP) module.

Parameters:

- in_channels (int) Number of channels of the input
- hidden_channels (List[int]) List of the hidden channel dimensions



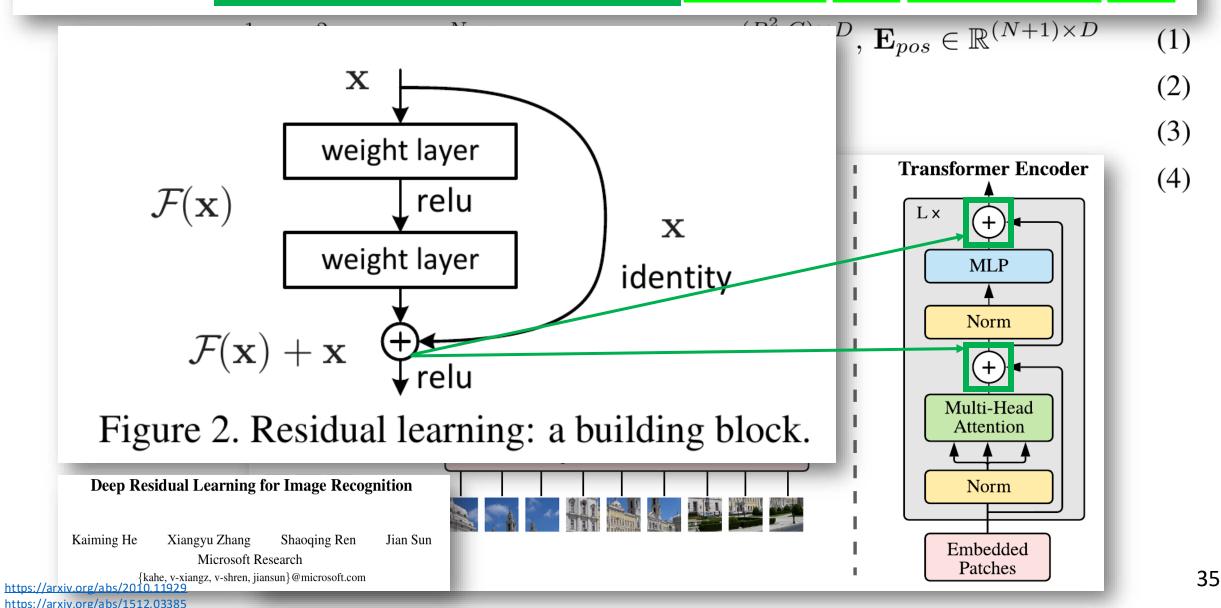
The Transformer encoder (Vaswani et al. 2017) consists of alternating layers of multiheaded self-attention (MSA, see Appendix A) and MLP blocks (Eq. 2 3). Layernorm (LN) is applied before every block, and residual connections after every block (Wang et al. 2019; Baevski & Auli 2019).

$$\mathbf{z}_{0} = [\mathbf{x}_{\text{class}}; \ \mathbf{x}_{p}^{1}\mathbf{E}; \ \mathbf{x}_{p}^{2}\mathbf{E}; \cdots; \ \mathbf{x}_{p}^{N}\mathbf{E}] + \mathbf{E}_{pos}, \qquad \mathbf{E} \in \mathbb{R}^{(P^{2} \cdot C) \times D}, \ \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$$
 (1)
$$\mathbf{z}'_{\ell} = \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1}, \qquad \ell = 1 \dots L$$
 (2)
$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z}'_{\ell})) + \mathbf{z}'_{\ell}, \qquad \ell = 1 \dots L$$
 (3)
$$\mathbf{y} = \text{LN}(\mathbf{z}_{L}^{0})$$
 Vision Transformer (VI)
$$\mathbf{y} = \text{LN}(\mathbf{z}_{L}^{0})$$

$$\mathbf{z} = \mathbf{z}_{L}^{0}$$

$$\mathbf{z}$$

The Transformer encoder (Vaswani et al. 2017) consists of alternating layers of multiheaded self-attention (MSA, see Appendix A) and MLP blocks (Eq. 2 3). Layernorm (LN) is applied before every block, and residual connections after every block (Wang et al., 2019; Baevski & Auli 2019).



The Transformer encoder (Vaswani et al. 2017) consists of alternating layers of multiheaded self-attention (MSA, see Appendix A) and MLP blocks (Eq. 2 3). Layernorm (LN) is applied before every block, and residual connections after every block (Wang et al. 2019; Baevski & Auli 2019).

$$\mathbf{z}_{0} = [\mathbf{x}_{\text{class}}; \ \mathbf{x}_{p}^{1}\mathbf{E}; \ \mathbf{x}_{p}^{2}\mathbf{E}; \cdots; \ \mathbf{x}_{p}^{N}\mathbf{E}] + \mathbf{E}_{pos}, \qquad \mathbf{E} \in \mathbb{R}^{(P^{2} \cdot C) \times D}, \ \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D} \tag{1}$$

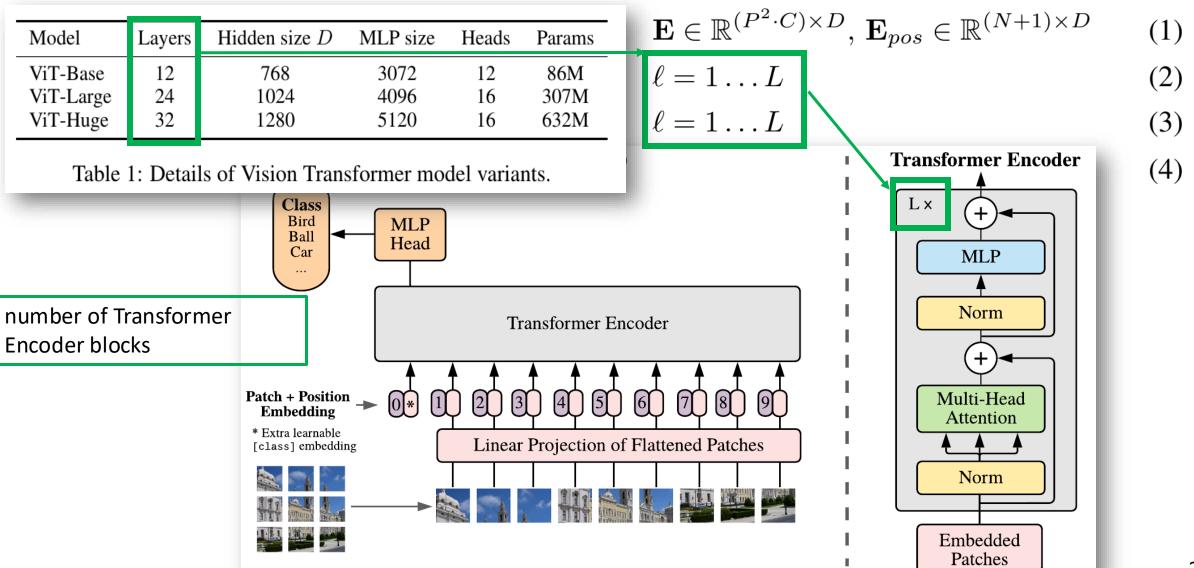
$$\mathbf{z}'_{\ell} = \text{MSA}(\text{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1}, \qquad \ell = 1 \dots L \tag{2}$$

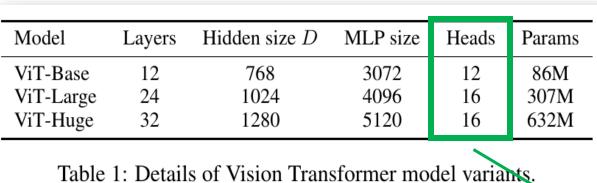
$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z}'_{\ell})) + \mathbf{z}'_{\ell}, \qquad \ell = 1 \dots L \tag{3}$$

$$\mathbf{y} = \mathbf{LN}(\mathbf{z}_{L}^{0}) \qquad \mathbf{Vision Transformer (ViT)} \qquad \mathbf{Transformer Encoder}$$

$$\mathbf{y} = \mathbf{LN}(\mathbf{z}_{L}^{0}) \qquad \mathbf{Vision Transformer Encoder}$$

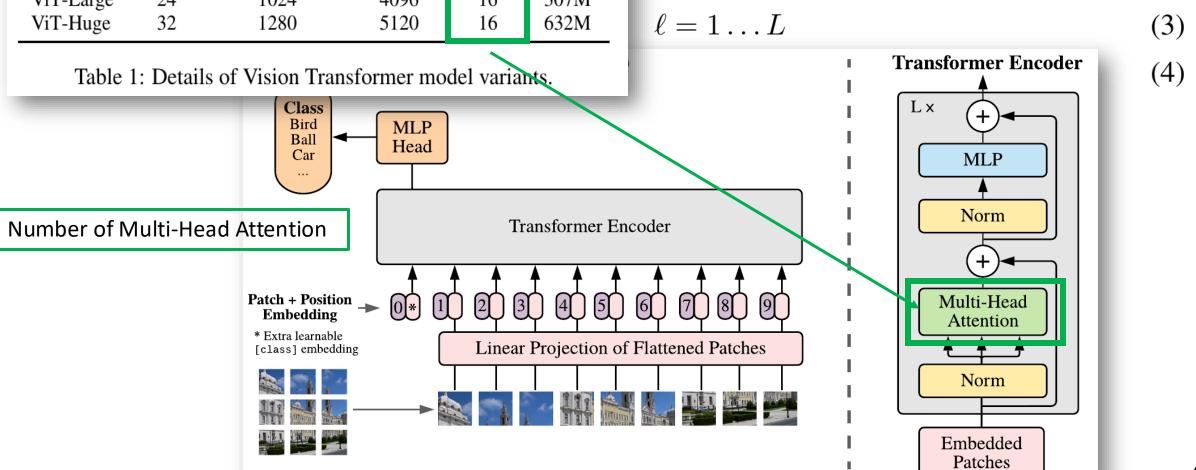
$$\mathbf{y} = \mathbf{LN}(\mathbf{z}_{L}^{0}) \qquad \mathbf{v} \qquad$$

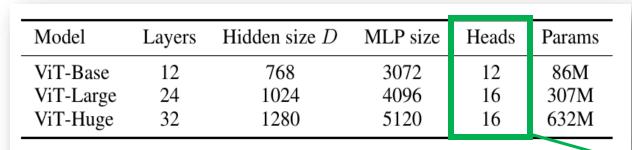






$$\ell = 1 \dots L \tag{2}$$







$$\ell = 1$$

$$\ell = 1$$

Table 1: Details of Vision Transformer model variants.

Class Bird **MLP** Ball Head Car

Number of Multi-Head Attention

Attention Is All You Need

Ashish Vaswani* Google Brain avaswani@google.com

Llion Jones*

Google Research

llion@google.com

Noam Shazeer* Google Brain noam@google.com

Niki Parmar* Google Research nikip@google.com

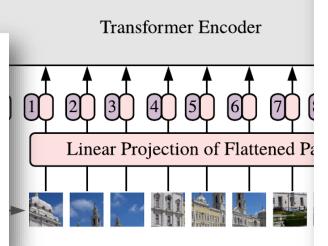
Jakob Uszkoreit* Google Research

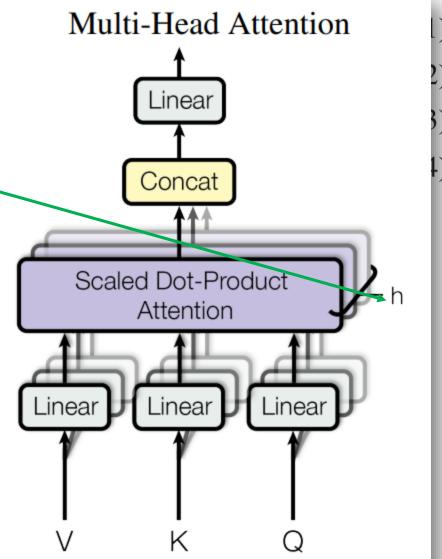
Aidan N. Gomez* † University of Toronto aidan@cs.toronto.edu

Łukasz Kaiser* Google Brain lukaszkaiser@google.com

Illia Polosukhin* 1

illia.polosukhin@gmail.com





A MULTIHEAD SELF-ATTENTION

Standard \mathbf{qkv} self-attention (SA, Vaswani et al. (2017)) is a popular building block for neural architectures. For each element in an input sequence $\mathbf{z} \in \mathbb{R}^{N \times D}$, we compute a weighted sum over all values \mathbf{v} in the sequence. The attention weights A_{ij} are based on the pairwise similarity between two elements of the sequence and their respective query \mathbf{q}^i and key \mathbf{k}^j representations.

$$[\mathbf{q}, \mathbf{k}, \mathbf{v}] = \mathbf{z} \mathbf{U}_{qkv} \qquad \qquad \mathbf{U}_{qkv} \in \mathbb{R}^{D \times 3D_h}, \qquad (5)$$

$$A = \operatorname{softmax}\left(\mathbf{q}\mathbf{k}^{\top}/\sqrt{D_h}\right) \qquad A \in \mathbb{R}^{N \times N},$$

$$SA(\mathbf{z}) = A\mathbf{v} \,. \tag{7}$$

Multihead self-attention (MSA) is an extension of SA in which we run k self-attention operations, called "heads", in parallel, and project their concatenated outputs. To keep compute and number of parameters constant when changing k, D_h (Eq. 5) is typically set to D/k.

$$MSA(\mathbf{z}) = [SA_1(z); SA_2(z); \cdots; SA_k(z)] \mathbf{U}_{msa}$$

$$\mathbf{U}_{msa} \in \mathbb{R}^{k \cdot D_h \times D} \tag{8}$$

illia.polosukhin@gmail.com

(6)

VisionTransformer

The VisionTransformer model is based on the An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale paper.

Model builders

The following model builders can be used to instantiate a VisionTransformer model, with or without pre-trained weights. All the model builders internally rely on the toxchvision.models.vision_transformer.VisionTransformer base class. Please refer to the source code for more details about this class.

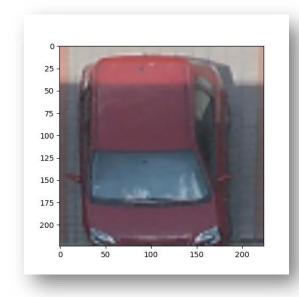
<pre>vit_b_16(*[, weights, progress])</pre>	Constructs a vit_b_16 architecture from An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale.
<pre>vit_b_32(*[, weights, progress])</pre>	Constructs a vit_b_32 architecture from An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale.
<pre>vit_1_16(*[, weights, progress])</pre>	Constructs a vit_l_16 architecture from An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale.
<pre>vit_1_32(*[, weights, progress])</pre>	Constructs a vit_l_32 architecture from An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale.
<pre>vit_h_14(*[, weights, progress])</pre>	Constructs a vit_h_14 architecture from An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale.

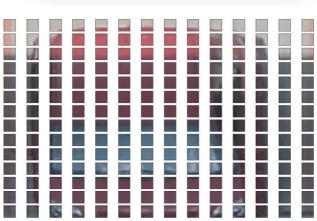
		ViT-B/16	ViT-B/32	ViT-L/16	ViT-L/32	ViT-H/14
ImageNet	CIFAR-10	98.13	97.77	97.86	97.94	-
	CIFAR-100	87.13	86.31	86.35	87.07	-
	ImageNet	77.91	73.38	76.53	71.16	-
	ImageNet ReaL	83.57	79.56	82.19	77.83	-
	Oxford Flowers-102	89.49	85.43	89.66	86.36	-
	Oxford-IIIT-Pets	93.81	92.04	93.64	91.35	-
ImageNet-21k	CIFAR-10	98.95	98.79	99.16	99.13	99.27
	CIFAR-100	91.67	91.97	93.44	93.04	93.82
	ImageNet	83.97	81.28	85.15	80.99	85.13
	ImageNet ReaL	88.35	86.63	88.40	85.65	88.70
	Oxford Flowers-102	99.38	99.11	99.61	99.19	99.51
	Oxford-IIIT-Pets	94.43	93.02	94.73	93.09	94.82
JFT-300M	CIFAR-10	99.00	98.61	99.38	99.19	99.50
	CIFAR-100	91.87	90.49	94.04	92.52	94.55
	ImageNet	84.15	80.73	87.12	84.37	88.04
	ImageNet ReaL	88.85	86.27	89.99	88.28	90.33
	Oxford Flowers-102	99.56	99.27	99.56	99.45	99.68
	Oxford-IIIT-Pets	95.80	93.40	97.11	95.83	97.56

Table 5: Top1 accuracy (in %) of Vision Transformer on various datasets when pre-trained on ImageNet, ImageNet-21k or JFT300M. These values correspond to Figure 3 in the main text. Models are fine-tuned at 384 resolution. Note that the ImageNet results are computed without additional techniques (Polyak averaging and 512 resolution images) used to achieve results in Table 2.

Part 3. Selected Implementation Details

We can use the **nn.Conv2d** layer to split the input image into patches (blocks) and create the embedding vector (with size = 768, in this example – ViT Base model) for each patch.

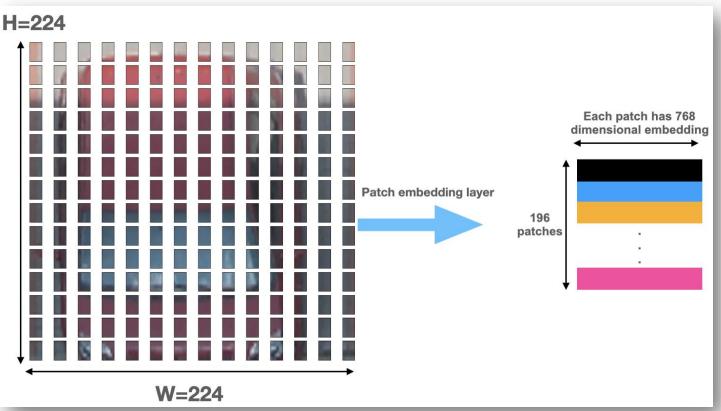




```
h = 224
W = 224
c = 3
ps = 16
conv = nn.Conv2d(
in channels = 3,
out channels = 768,
kernel size = (ps,ps),
stride
            = ps,
padding
            = 0,
            = False)
bias
```

shape of input 224 x 244 x 3 image after nn.Conv2d: ([768, 14, 14])

- 768 feature maps of size 14 x 14 are generated
- we can use flatten on these 14 x 14 feature maps to obtain: ([batch_size, 768, 196])
- it is necessary to switch dimensions so that the number of patches is in the second place: ([batch_size, 196, 768])



- class_token = nn.Parameter(torch.ones(batch_size, 1, 768))
- z_0_with_class = torch.cat((class_token, block_out_permute), dim=1)
- position_embeddings = nn.Parameter(torch.ones(1, 197, 768))
- z_0_with_class_with_poss = z_0_with_class + position_embeddings

$$\mathbf{z}_0 = [\mathbf{x}_{\text{class}}; \mathbf{x}_p^1 \mathbf{E}; \mathbf{x}_p^2 \mathbf{E}; \cdots; \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos},$$

$$\mathbf{z}'_{\ell} = MSA(LN(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1},$$

$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z'}_{\ell})) + \mathbf{z'}_{\ell},$$

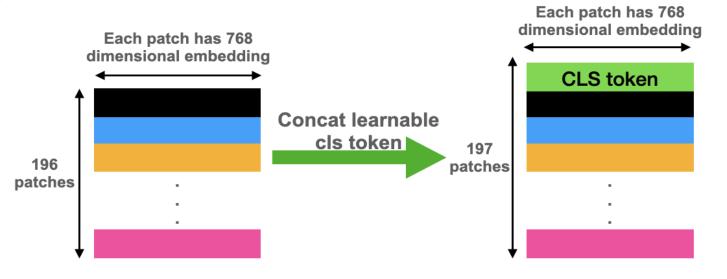
$$\mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$$



$$\ell = 1 \dots L \tag{2}$$

$$\ell = 1 \dots L \tag{3}$$

block_permute = nn.Sequential(



```
nn.Conv2d(
in_channels=3,
out_channels=768,
kernel_size=(ps,ps),
stride=ps,
padding = 0,
bias=False),
nn.Flatten(start_dim=2, end_dim=-1),
MyPermute((0, 2, 1))
```

- class token = nn.Parameter(torch.ones(batch_size, 1, 768))
- z 0 with_class = torch.cat((class_token, block_out_permute), dim=1)
- position_embeddings = nn.Parameter(torch.ones(1, 197, 768))
- z 0 with class with poss = z 0 with class + position embeddings

$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \ \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{x}_p^2 \mathbf{E}; \cdots; \ \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos},$$

$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \ \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{x}_p^2 \mathbf{E}; \cdots; \ \mathbf{x}_p^N \mathbf{E}] + [\mathbf{E}_{pos},]$$

$$\mathbf{z}'_{\ell} = MSA(LN(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1},$$

$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z'}_{\ell})) + \mathbf{z'}_{\ell},$$

$$\mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$$

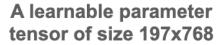
 $\mathbf{E} \in \mathbb{R}^{(P^2 \cdot C) \times D}, \, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$ (1)

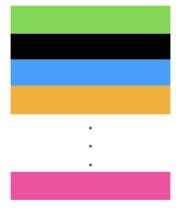
$$\ell = 1 \dots L \tag{2}$$

$$\ell = 1 \dots L$$

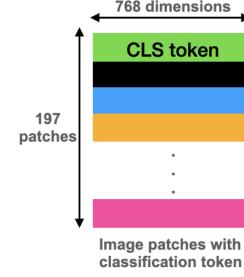


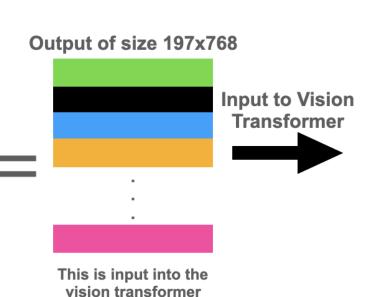
(3)











Position embedding

- class_token = nn.Parameter(torch.ones(batch_size, 1, 768))
- z_0_with_class = torch.cat((class_token, block_out_permute), dim=1)
- position_embeddings = nn.Parameter(torch.ones(1, 197, 768))
- z_0_with_class_with_poss = z_0_with_class + position_embeddings

$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \, \mathbf{x}_p^1 \mathbf{E}; \, \mathbf{x}_p^2 \mathbf{E}; \cdots; \, \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos},$$

$$\mathbf{z}'_{\ell} = MSA(LN(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1},$$

$$\mathbf{z}_{\ell} = \text{MLP}(\text{LN}(\mathbf{z'}_{\ell})) + \mathbf{z'}_{\ell},$$

$$\mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$$

 $\mathbf{E} \in \mathbb{R}^{(P^2 \cdot C) \times D}, \, \mathbf{E}_{pos} \in \mathbb{R}^{(N+1) \times D}$ (1)

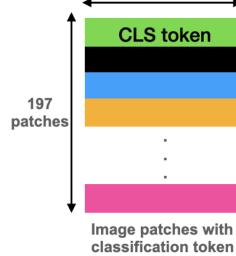
$$\ell = 1 \dots L \tag{2}$$

$$\ell=1\dots L$$

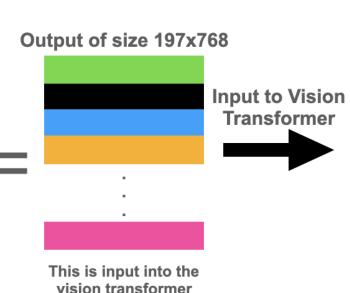








768 dimensions



Position embedding

(3)

/ **/** \

MultiheadAttention

CLASS torch.nn.MultiheadAttention(embed_dim, num_heads, dropout=0.0, bias=True,

add_bias_kv=False, add_zero_attn=False, kdim=None, vdim=None, batch_first=False,

device=None, dtype=None) [SOURCE]

Allows the model to jointly attend to information from different representation subspaces.

Method described in the paper: Attention Is All You Need.

Multi-Head Attention is defined as:

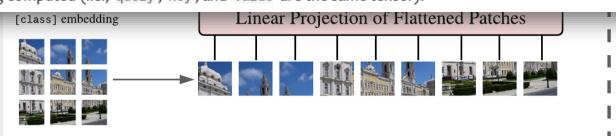
$$MultiHead(Q, K, V) = Concat(head_1, ..., head_h)W$$

where $head_i = Attention(QW_i^Q, KW_i^K, VW_i^V)$.

nn.MultiHeadAttention will use the optimized implementations of scaled_dot_product_attention() when possible.

In addition to support for the new scaled_dot_product_attention() function, for speeding up Inference, MHA will use
fastpath inference with support for Nested Tensors, iff:

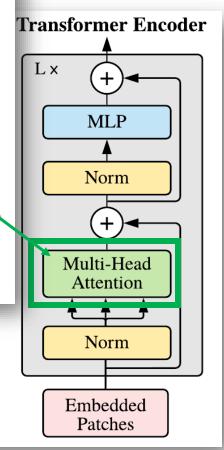
• self attention is being computed (i.e., query, key, and value are the same tensor).

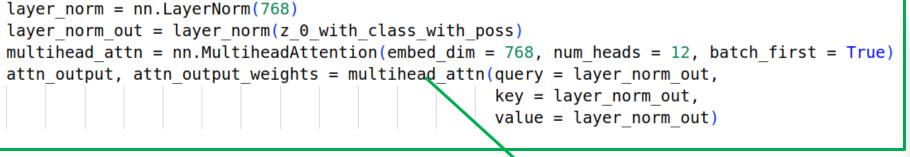


sformer)

$$p_{oos} \in \mathbb{R}^{(N+1) \times D}$$
 (1)

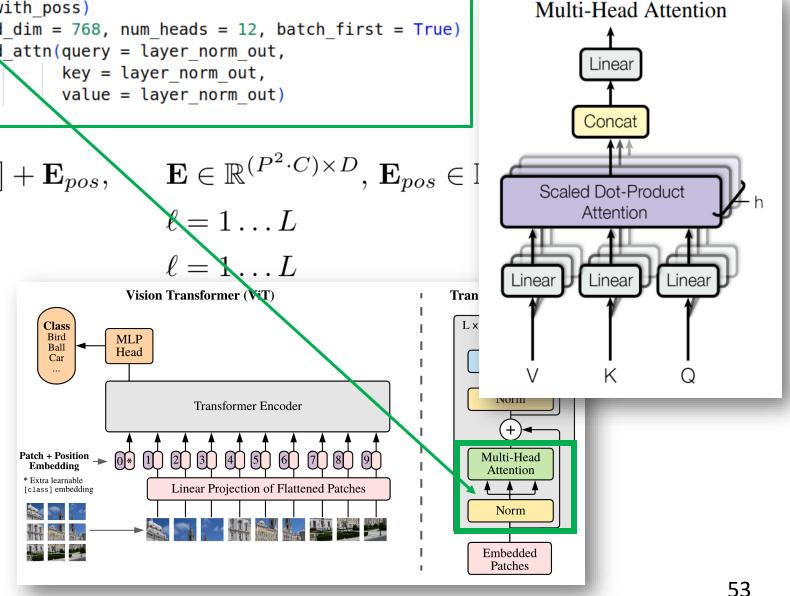
- (2)
- (3)
- (4)





$$\mathbf{z}_0 = [\mathbf{x}_{\mathrm{class}}; \ \mathbf{x}_p^1 \mathbf{E}; \ \mathbf{x}_p^2 \mathbf{E}; \cdots; \ \mathbf{x}_p^N \mathbf{E}] + \mathbf{E}_{pos},$$
 $\mathbf{z'}_\ell = \mathrm{MSA}(\mathrm{LN}(\mathbf{z}_{\ell-1})) + \mathbf{z}_{\ell-1},$
 $\mathbf{z}_\ell = \mathrm{MLP}(\mathrm{LN}(\mathbf{z'}_\ell)) + \mathbf{z'}_\ell,$
 $\mathbf{y} = \mathrm{LN}(\mathbf{z}_L^0)$

You can continue in a similar way with equations 3 and 4 during the exercise (it is appropriate to organise the ViT blocks into individual classes)



Where to go from here?

https://github.com/lucidrains/vit-pytorch

